

Investor Sentiment

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平均報酬率

- 錯誤的算法：算術平均。

第1年報酬率=100%、第2年報酬率=-60% ，
平均報酬率=(100%-60%)/2 = 20% ?

- 平均報酬率的計算方式：幾何平均

$$\bar{R} = \left[(1 + R_1)(1 + R_2) \dots (1 + R_N) \right]^{\frac{1}{N}} - 1 = \left[\prod_{t=1}^N (1 + R_t) \right]^{\frac{1}{N}} - 1$$

R_t ：第t期的報酬率

\bar{R} ：1到N期的平均報酬率

風險：報酬率標準差

- 風險是指報酬率的不確定性，一般以標準差 (standard deviation)，報酬率標準差的計算方式如下：

$$\sigma = \sqrt{\frac{1}{N} \sum_{t=1}^N (R_t - \bar{R})^2}$$

Σ ：1到N期的報酬率標準差

R_t ：第t期的報酬率

\bar{R} ：到N期的平均報酬率

基本定裡

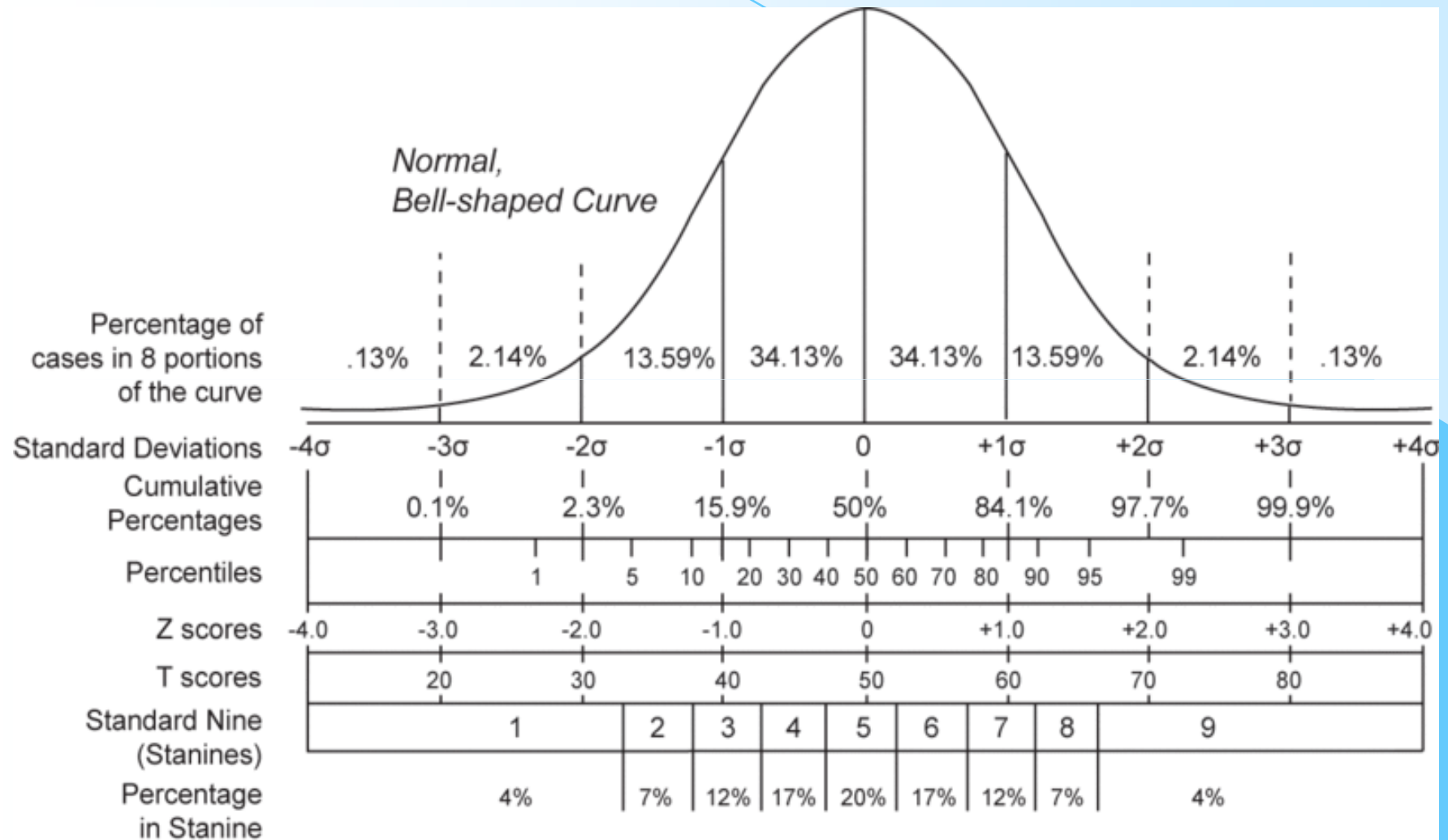
- 1年有250交易日，年平均報酬率= 10% ，年平均報酬率標準差=18% 。日平均報酬率 \doteq 0.04% (大約為10%/250)，日平均報酬率標準差 \doteq 0.114% (18%/ $\sqrt{250}$) 。

$$\mu_N = \frac{1}{N} \mu \qquad \sigma_N = \frac{1}{\sqrt{N}} \sigma$$

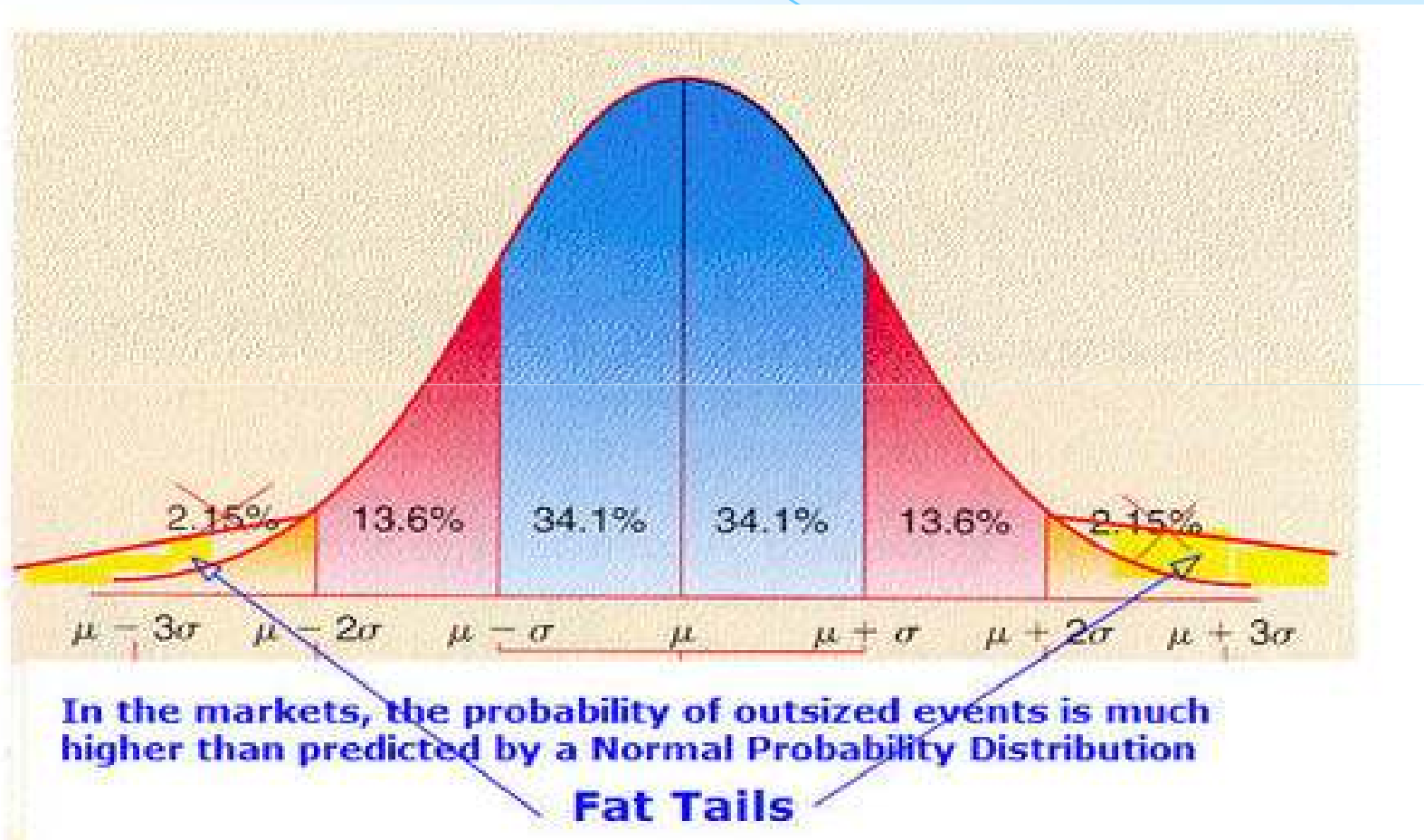
Shit Happens!

- 報酬率的機率分佈：
 - Normal Distribution?
 - Fat Tail Distribution?

Normal Distribution



Fat Tail Distribution



Big Bang: 150億年前 (年前) , Benchmark: 1.5×10^{10}

a. $|X - \mu| \geq 5\sigma = 2 \times 0.287 \times 10^{-6}$

Assume: 250 trading days per year \rightarrow 7000 Years

b. 1998.08.04: -3.5%

08.25: -4.4%

08.31: -6.8%

1998.08.31: Probability = $\frac{1}{2 \times 10^7} = \frac{1}{2000\text{萬}}$ \rightarrow 80,000 Years

1998.08.04 + 08.25 + 08.31: Probability = $\frac{1}{5000 \times 10^8} = \frac{1}{5000\text{億}}$

\rightarrow 2,000,000,000 Years

c. 1987.10.19: -29.2%

Probability = $\frac{1}{10^{50}}$ \rightarrow 4×10^{47} Years

Manias / Panics

Mob. Psychology

Rational individuals and irrational whole.

BOE:1694

1.2M £ × 8% + 4000 £

Governor and the Company of the Bank of England.

1.群眾不理性與善變

irrationality & vicissitude of the crowd. Martin

2.herding and winner's curse: 個人的行為，會受到他人的影響。

Newton. South Sea Company：成立於1711年

中南美洲貿易

BOE.

心理實驗

自我實現的預期

a. 1720年，接受認股

Banker (Martin) . 認購 £ 500

“When the rest of the world are mad, we must imitate them in some measure”.

b.* Issac Newton, 1720年Spring:

“I can calculate the motions of the heavenly bodies, but not the madness of people”.

* 1720年4月20日，出清South Sea股票，獲利 £ 7000 (100%)

* Summer: 再度投資，損失 £ 20,000

1841年，

Charles Mackay, Extraordinary Popular Delusions and the Madness of Crowds.

BOE

S.E.: Proposed 6% → 5%

結果，1720 proposed to take over £ 30,981,712 (3千1百萬 £) for 5% until 1727.

發行股票，給10%股利

Bubble Company 競相發行股票 → 資金排擠 → S.E. 請求政府取締 → Burst the Bubbles



Tronics Boom

1959-1962:

IPO Craze

Astron

Dutron

Vulcatron

Transitron

Circuitronics

Supronics

Videotronics

P/E Miracle

P/E for “ Shoelaces Inc. “ is 6.

“Electronics & Silicon Fourth – Burners” has a P/E of 42

1. Reward / Risk Ratio = $\frac{\overline{R_P}}{\sigma_P}$

2. Treynor Index = $\frac{\overline{R_P} - \overline{R_F}}{\beta_P}$, $\overline{R_P} - \overline{R_F}$ = Risk Premium

3. Sharpe Index = $\frac{\overline{R_P} - \overline{R_F}}{\sigma_P}$, $\overline{R_P} - \overline{R_F}$ = Risk Premium

4. Jensen Index = Jensen's α

$$(\overline{R_P} - \overline{R_F}) = \alpha_p + \beta_P \times (\overline{R_m} - \overline{R_F})$$